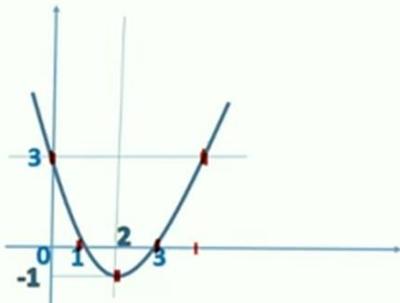


1. 1) $f(x) = x^2 - 4x + 3$ funksiya grafigini yasang

$$x_0 = -\frac{b}{2a} = -\frac{-4}{2 \cdot 1} = 2. \quad y_0 = 2^2 - 4 \cdot 2 + 3 = -1 \quad (2;-1)$$

$$x^2 - 4x + 3 = 0 \quad x_1 = 3, \quad x_2 = 1$$



$$f(0) = f(4) = 3$$

1. 2) Hisoblang: $\log_{3\sqrt{3}} 27 + \log_{\sqrt{5}} 125$

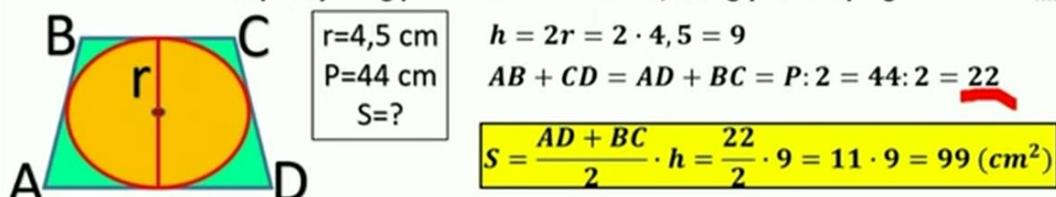
$$\log_{3\sqrt{3}} 27 + \log_{\sqrt{5}} 125 = \log_{3^{1.5}} 3^3 + \log_{5^{0.5}} 5^3 = \frac{3}{1.5} + \frac{3}{0.5} = 2 + 6 = 8$$

1. 3) $\sin x + \sqrt{3} \cos x = 2$. Tenglamani yeching:

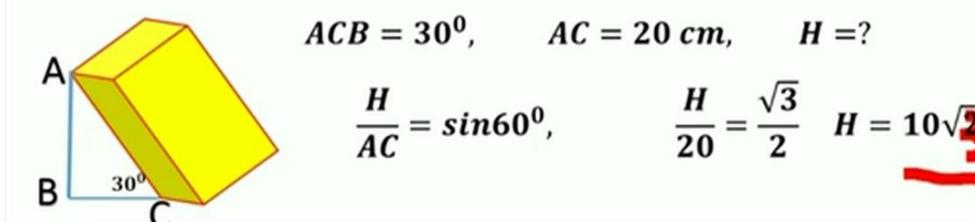
$$\frac{1}{2} \sin x + \frac{\sqrt{3}}{2} \cos x = 1 \quad \cos \frac{\pi}{3} \sin x + \sin \frac{\pi}{3} \cos x = 1$$

$$\sin \left(\frac{\pi}{3} + x \right) = 1. \quad \frac{\pi}{3} + x = \frac{\pi}{2} + 2k\pi \quad x = \frac{\pi}{6} + 2k\pi, \quad k \in \mathbb{Z}$$

1.4. Teng yonli trapetsiyaga radiusi 4,5 cm bo'lgan aylana ichki chizilgan. Agar trapetsyaning perimetri 44 cm bo'sa, uning yuzini toping.



1.5. Og'ma prizmaning 20 cm ga teng bo'lgan yon qirrasi asos tekisligi bilan 60° li burchak tashkil etadi. Prizmaning balandligi necha cm ga teng?



11 sinf 2 belet

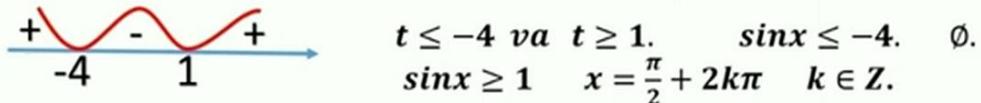
2.1) Tenglamani yeching: $3^{x^2-7x} = \frac{1}{729}$

$$3^{x^2-7x} = 3^{-6} \quad x^2 - 7x = -6, \quad x^2 - 7x + 6 = 0, \quad x_1 = 1, x_2 = 6$$



2.2) Tengsizlikni yeching: $\sin^2 x + 3\sin x - 4 \geq 0$.

$$\sin x = t, \quad t^2 + 3t - 4 \geq 0, \quad (t+4)(t-1) \geq 0$$



2.3) $f(x) = \sin x \cos 3x$ funksiya hosilasini toping.

$$f'(x) = \cos x \cos 3x + \sin x (-3\sin 3x) = \cos x \cos 3x - 3\sin x \sin 3x$$

2.4) Katetlari 6 cm va 8 cm ga teng bo'lgan to'g'ri burchakli uchburchakka ichki chizilgan doira yuzini toping.



A

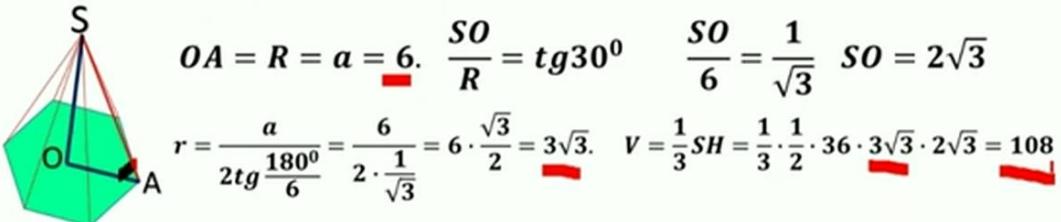
$$BC = 6 \text{ cm}, \quad AC = 8 \text{ cm}, \quad S_r = ?$$

$$AB = \sqrt{6^2 + 8^2} = \sqrt{100} = 10, \quad r = \frac{AC + BC - AB}{2} = \frac{8 + 6 - 10}{2} = 2$$

C

$$S = 4\pi$$

2.5) Piramidaning asosi tomoni 6 ga teng bo'lgan muntazam oltiburchakdan iborat bo'lib, barcha yon qirralari asos tekisligi bilan 30° li burchak tashkil etadi. Piramida hajmini toping.



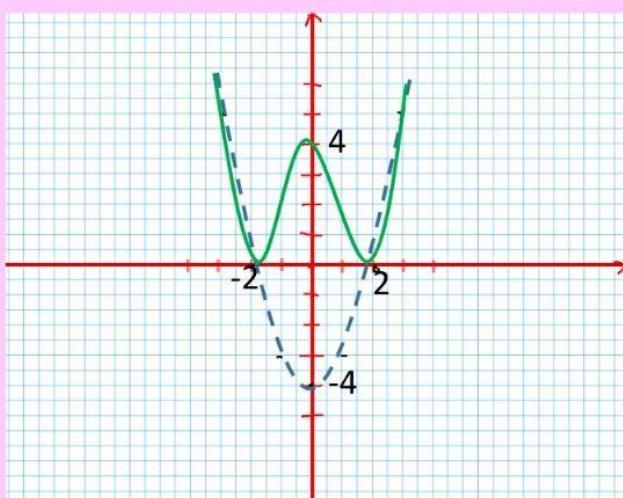
11 sinf 3 belet

3-BILET

1. Ifodani soddalashtiring: $\left(\frac{\sqrt{a}}{b+\sqrt{ab}} - \frac{\sqrt{a}}{b-\sqrt{ab}} \right) \cdot \frac{b-a}{2\sqrt{ab}}$.

$$\begin{aligned} &= \left(\frac{\sqrt{a}}{\sqrt{b}(\sqrt{b} + \sqrt{a})} - \frac{\sqrt{a}}{\sqrt{b}(\sqrt{b} - \sqrt{a})} \right) \cdot \frac{b-a}{2\sqrt{ab}} = \\ &= \frac{\sqrt{a}(\sqrt{b} - \sqrt{a}) - \sqrt{a}(\sqrt{b} + \sqrt{a})}{\sqrt{b}(b-a)} \cdot \frac{b-a}{2\sqrt{ab}} = \\ &\frac{\sqrt{ab} - a - \sqrt{ab} - a}{\sqrt{b}} \cdot \frac{1}{2\sqrt{ab}} = \frac{-2a}{2b\sqrt{a}} = -\frac{\sqrt{a}}{b} \end{aligned}$$

2. $f(x) = |x^2 - 4|$ funksiya grafigini yasang.

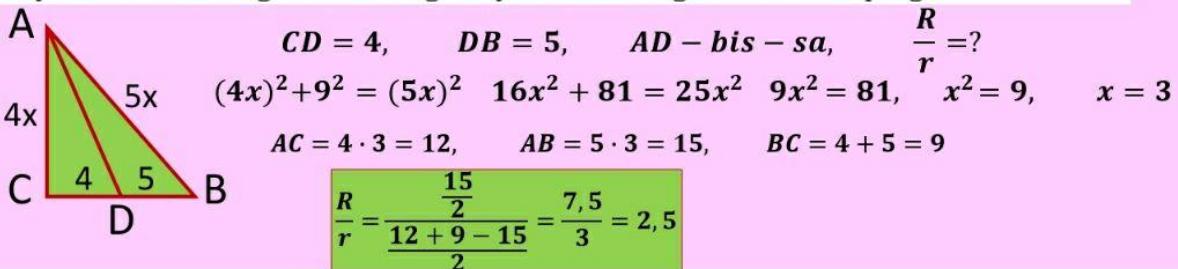


3. $f(x) = \cos 5x \cdot \cos 2x$ funksiya boshlang'ich funksiyasini toping.

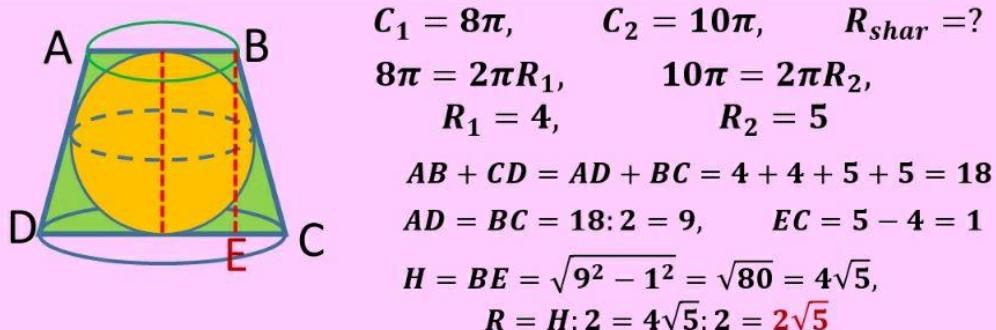
$$\cos x \cos y = \frac{1}{2} (\cos(x+y) + \cos(x-y)). \quad f(x) = \frac{1}{2} (\cos 7x + \cos 3x)$$

$$F(x) = \frac{1}{2} \left(\frac{1}{7} \sin 7x + \frac{1}{3} \sin 3x \right) + C = \frac{1}{14} \cos 7x + \frac{1}{6} \sin 3x + C$$

4. To'g'ri burchakli uchburchakning kichik katetiga tushirilgan bissektrisasi uni 4 cm va 5 cm li kesmalarga ajratadi. Bu uchburchakka tashqi chizilgan aylana radiusining ichki chizilgan aylana radiusiga nisbatini toping.

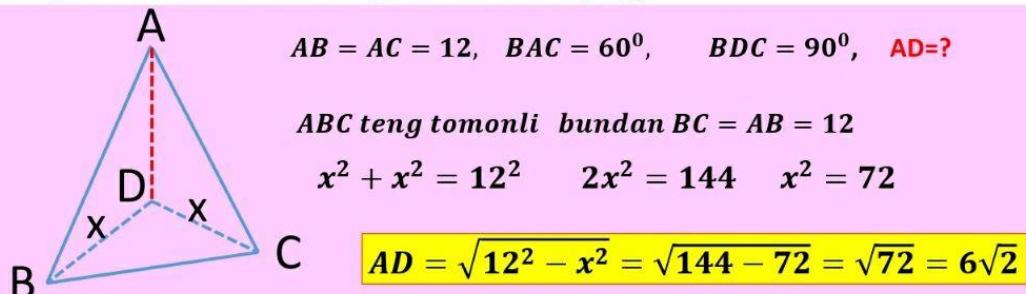


5. Kesik konusga shar ichki chizilgan. Kesik konus asoslari aylanalarining uzunliklari 8π cm va 10π cm ga teng bo'lsa, shar radiusini toping.



11 sinf 4 belet

5. Tekislikda yotmaydigan nuqtadan tekislikka uzunliklari 12 cm dan va orasidagi burchak 60° ga teng bo'lgan ikkita og'malar o'tkazilgan. Agar og'malarning tekislikdagi proyeksiyalari o'zaro perpendikulyar bo'lsa, nuqtadan tekislikkacha bo'lgan masofani toping.



4-BILET

1. Ko'phadni ko'paytuvchilarga ajrating: $(x^2 + x)^2 - 8(x^2 + x) + 12$.

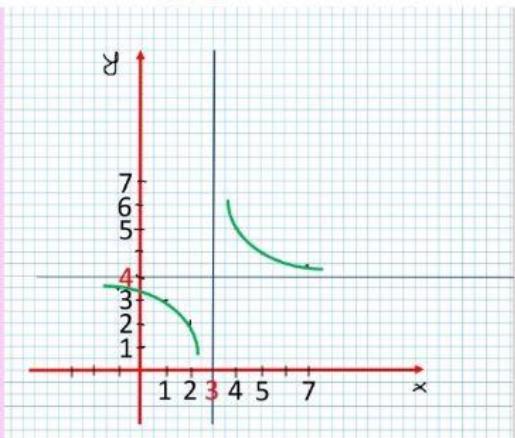
$$x^2 + x = t$$

$$t^2 - 8t + 12 = (t - 6)(t - 2) = (x^2 + x - 6)(x^2 + x - 2)$$

2. Savatda 5 ta qizil, 4 ta sariq, 4 ta oq gul bor. 2 ta qizil, 2 ta oq, 2 ta sariq guldan iborat bo'lgan guldastani necha xil usulda tayyorlash mumkin.

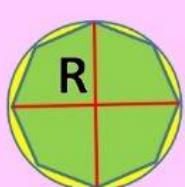
$$C_5^2 \cdot C_4^2 \cdot C_4^2 = \frac{5 \cdot 4}{1 \cdot 2} \cdot \frac{4 \cdot 3}{1 \cdot 2} \cdot \frac{4 \cdot 3}{1 \cdot 2} = 10 \cdot 6 \cdot 6 = 360$$

3. $f(x) = \frac{2}{x-3} + 4$ funksiya grafigini yasang.



x	y
1	3
2	2
-1	3,5
4	6
5	5
7	4,5

4. Muntazam sakkizburchak va oltiburchaklarning eng katta diagonallari teng. Ularning yuzlari nisbatini toping.



$$r = R \cos \frac{180^\circ}{n}$$

$$a = 2R \sin \frac{180^\circ}{n}$$

$$a_8 = 2R \sin \frac{180^\circ}{8} = 2R \sin 22,5^\circ \quad a_6 = 2R \sin \frac{180^\circ}{6} = 2R \sin 30^\circ = R$$

$$r_1 = R \cos 22,5^\circ \quad r_2 = R \cos 30^\circ = \frac{R}{2}$$

$$S_1 = \frac{1}{2} \cdot 8 \cdot 2R \sin 22,5^\circ \cdot R \cos 22,5^\circ = 4R^2 \sin 45^\circ = 4R^2 \cdot \frac{\sqrt{2}}{2} = 2\sqrt{2}R^2$$

$$S_2 = \frac{1}{2} \cdot 6 \cdot R \cdot \frac{R}{2} = \frac{3R^2}{2}$$

$$\frac{S_1}{S_2} = 2\sqrt{2}R^2 \cdot \frac{2}{3R^2} = \frac{4\sqrt{2}}{3}$$

11 sınıf 5 belet

5. Bilet

$$1. 5x^2 - 29x + 20 \leq 0$$

$$5x^2 - 29x + 20 = 0$$

$$\Delta = 29^2 - 4 \cdot 5 \cdot 20 = 841 - 400 = 441$$

$$5(x-5)(x-0,8) \leq 0$$

$$0,8 \leq x \leq 5$$

$$x_1 = \frac{29+21}{2 \cdot 5} = 5$$

$$x_2 = \frac{29-21}{10} = 0,8$$

$$\begin{array}{c} + \\ - \\ \hline 0,8 & 5 \end{array}$$

$$\frac{1+2+3+4+5}{5} = \frac{15}{5} = 3 \quad \text{J: 3}$$

$$2. b_4 - 9b_2 + b_3 - 9b_1 = 0$$

$$b_1 8^3 - 9b_1 8 + b_1 8^2 - 9b_1 = 0$$

$$b_1 8^2(8+1) - 9b_1(8+1) = 0$$

$$(8+1)(b_1 8^2 - 9b_1) = 0$$

$$1) 8 = -1 \quad 2) b_1 8^2 - 9b_1 = 0$$

$$b_1(8^2 - 9) = 0$$

$$b_1 = 0 \quad 8^2 - 9 = 0$$

$$8^2 = 9$$

$$g = \pm 3$$

$$\text{J: } g = 3$$

$$3) \frac{(\cot 44^\circ + \tan 226^\circ) \cdot \cot 406^\circ + \tan(-405^\circ)}{\cot 316^\circ} =$$

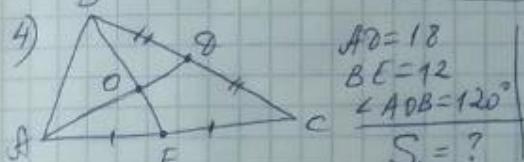
$$= \frac{(\cot 44^\circ + \tan(120^\circ + 46^\circ)) \cdot \cot(360^\circ + 46^\circ)}{\cot(360^\circ - 44^\circ)}$$

$$+ \tan(360^\circ + 45^\circ) =$$

$$= \frac{(\tan 46^\circ + \tan 46^\circ) \cdot \cot 46^\circ}{\cot 44^\circ} - \tan 45^\circ =$$

$$= \frac{2 \sin 46^\circ}{\sin 46^\circ} - 1 = 2 - 1 = 1$$

$$\text{J: 1}$$



$$AO = 12$$

$$BE = 12$$

$$\angle AOB = 120^\circ$$

$$S_A = ?$$

Yerel hiz: :

$$BO : OE = 2 : 1 \Rightarrow BO = 8 \quad OE = 4$$

$$AO : OD = 2 : 1 \Rightarrow AO = 12 \quad OD = 6$$

$$S_A = 2 \cdot S_{ABE}$$

$$S_{ABO} = \frac{1}{2} \cdot 8 \cdot 12 \cdot \sin 120^\circ = 48 \cdot \frac{\sqrt{3}}{2} = 24\sqrt{3}$$

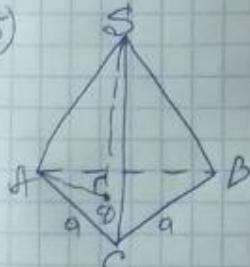
$$S_{AOE} = \frac{1}{2} \cdot 12 \cdot 4 \sin 60^\circ =$$

$$= 24 \cdot \frac{\sqrt{3}}{2} = 12\sqrt{3}$$

$$S_{ABE} = 24\sqrt{3} + 12\sqrt{3} = 36\sqrt{3}$$

$$S_{AAC} = 2 \cdot 36\sqrt{3} = 72\sqrt{3} \quad \text{J: } 72\sqrt{3}$$

5)



$$SA = SC = a$$

$$H = ?$$

Yerel hiz: :

$$S_{\text{orts}} = \frac{a^2\sqrt{3}}{4}$$

$$AD = R = \frac{a}{2 \sin 60^\circ} = \frac{a}{2 \cdot \frac{\sqrt{3}}{2}} = \frac{a}{\sqrt{3}}$$

$$H = SD = \sqrt{SA^2 - AD^2} = \sqrt{a^2 - \left(\frac{a}{\sqrt{3}}\right)^2} = \sqrt{a^2 - \frac{a^2}{3}} =$$

$$= \sqrt{\frac{2a^2}{3}} = a\sqrt{\frac{2}{3}} \quad \text{J: } a\sqrt{\frac{2}{3}}$$

11 sınıf 6 belet

6. Bilet.

1) $0, 1, 3, 5, 7, 8$

4 xonali son.

$$\begin{array}{r} 9800 \\ \downarrow \downarrow \downarrow \downarrow \\ 5543 \end{array}$$

$$5 \cdot 5 \cdot 4 \cdot 3 = 25 \cdot 12 = 300$$

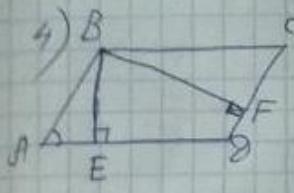
$\sqrt{300}$.

2) x_1 ve x_2 sonları $x^2 - ax + 20 = 0$ $\frac{1}{x_1} + \frac{1}{x_2} = \frac{9}{20}$, $a = ?$

$$x_1 + x_2 = a \quad x_1 \cdot x_2 = 20 \quad \frac{1}{x_1} + \frac{1}{x_2} = \frac{9}{20} \Rightarrow \frac{x_1 + x_2}{x_1 \cdot x_2} = \frac{9}{20} \Rightarrow$$

$$\Rightarrow 9x_1 \cdot x_2 = 20(x_1 + x_2) \Rightarrow 9 \cdot 20 = 20a \quad a = 9 \quad \sqrt{9}$$

3) $\sin(2 \arccos \frac{1}{3}) = 2 \sin(\arccos \frac{1}{3}) \cos(\arccos \frac{1}{3}) =$
 $= 2 \cdot \frac{1}{3} \cdot \sqrt{1 - (\frac{1}{3})^2} = \frac{2}{3} \cdot \sqrt{1 - \frac{1}{9}} = \frac{2}{3} \cdot \sqrt{\frac{8}{9}} = \frac{2}{3} \cdot \frac{2\sqrt{2}}{3} = \frac{4\sqrt{2}}{9};$



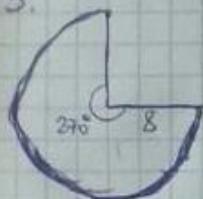
$$\begin{aligned} BE &= 8 \text{ cm} \\ BF &= 12 \text{ cm} \\ \angle A : \angle B &= 1 : 5 \\ S &=? \end{aligned}$$

Yekhislı:
 $\angle A = x \quad \angle B = 5x$
 $x + 5x = 180^\circ$
 $6x = 180^\circ$
 $x = 30^\circ \quad \angle A = 30^\circ$
 $\angle B = 150^\circ \quad \angle C = 30^\circ \quad \angle D = 150^\circ$

$$\angle A = 30^\circ \Rightarrow AB = 2 \cdot BE = 2 \cdot 8 = 16 \quad CD = 16$$

$$S = CD \cdot BF = 16 \cdot 12 = 192 \text{ cm}^2 \quad \sqrt{192} \text{ cm}^2$$

5.



$$S_{\text{yuk}} = \pi R l = S_{\text{lateral}}$$

$$S_{\text{yuk}} = \frac{\pi R^2}{360^\circ} \cdot 270^\circ = \frac{\pi \cdot 8^2}{4} \cdot 3 = 48\pi.$$

$$S_{\text{yuk}} = 48\pi \quad \pi \cdot R \cdot l = 48\pi$$

$$R = 6.$$

$$\triangle ABC \text{ da } AB = BC = 8 \quad AC = 2 \cdot 6 = 12.$$

$$OB = \sqrt{8^2 - 6^2} = \sqrt{64 - 36} = \sqrt{28} = 2\sqrt{7} \quad S_{\triangle ABC} = \frac{1}{2} \cdot 12 \cdot 2\sqrt{7} = 12\sqrt{7}.$$

~~$$\frac{abc}{4rs} = \frac{2S}{a+b+c} = \frac{2 \cdot 12\sqrt{7}}{8+8+12} = \frac{24\sqrt{7}}{28} = \frac{6\sqrt{7}}{7},$$~~

11 sinf 7 belet

7- bilet.

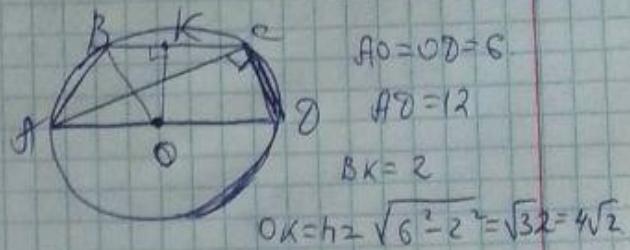
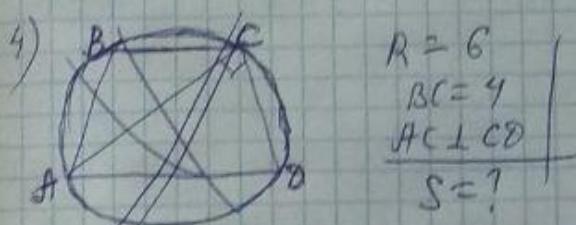
1) 1 day 75 jachy tub földönkívül 2020. m/2:
 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47,
 53, 59, 61, 67, 71, 73 — 21 db.
 $P(A) = \frac{21}{75} = \frac{7}{25}$; J: $\frac{7}{25}$.

2) $f(x) = 8x^3 - 5$ J: (1; 4)
 $F(x) = 8 \cdot \frac{x^4}{4} - 5x + C = 2x^4 - 5x + C$

$4 = 2 \cdot 1^4 - 5 \cdot 1 + C \quad C = 4 + 3 \quad C = 7.$

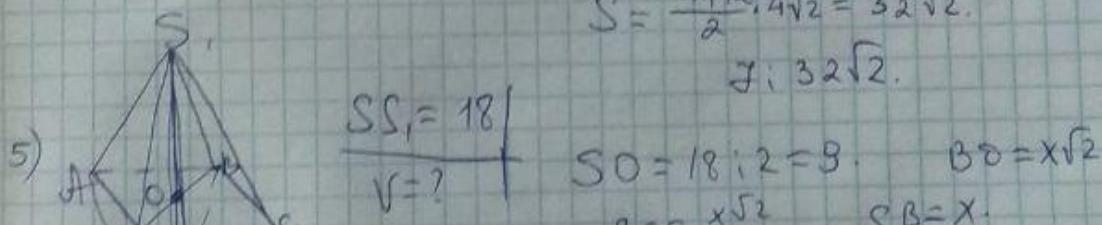
J: $F(x) = 2x^4 - 5x + 7.$

3) $\log_3(x-2) - \log_{\sqrt{3}}(\sqrt{x-4}) = 1$ $\log_3(x-2)(x-4) = \log_3^3$
 $\log_3(x-2) - \log_{3^{\frac{1}{2}}}((x-4)^{\frac{1}{2}}) = 1$ $x^2 - 6x + 8 = 3$
 $\log_3(x-2) + \log_3(x-4) = 1$ $x^2 - 6x + 5 = 0$
 $x_1 = 5$
 $x_2 = 1$. J: $x = 5$



$S = \frac{4+12 \cdot 4\sqrt{2}}{2} = 32\sqrt{2}.$

J: $32\sqrt{2}$.



$SO = 18 : 2 = 9$. $BD = x\sqrt{2}$

$BO = \frac{x\sqrt{2}}{2}$ $SB = x$.

$\triangle SOB$ dísz. $SO^2 + OB^2 = SB^2$

$$9^2 + \left(\frac{x\sqrt{2}}{2}\right)^2 = x^2 \quad 81 + \frac{x^2}{2} = x^2$$

$$\frac{x^2}{2} = 81 \quad x^2 = 162$$

$$x = 9\sqrt{2}$$

$S_{\text{hab}} = x^2 = 162$.

$V = 2 \cdot \frac{1}{3} \cdot S_{\text{hab}} \cdot h = \frac{2}{3} \cdot 162 \cdot 9 = 972$ J: 972.

8-BILET

1. $4^{x-3} = 2\sqrt{2^{\frac{3x-5}{3}}}$ tenglamani yeching.

$$2^{2(x-3)} = 2^{\frac{3(3x-5)}{3}}$$

2. $f(x) = 2 + 6\cos^2(2x+2)$ funksiyaning qiymatlar to'plamini toping.

$$2^{2x-6} = 2^{\frac{3x-5}{2}}$$

$$-1 \leq \cos x \leq 1 \quad 0 \leq \cos^2 x \leq 1$$

$$2x - 6 = \frac{3x - 5}{2}$$

$$f_{min}(x) = 2 + 6 \cdot 0 = 2 \quad va \quad f_{max}(x) = 2 + 6 \cdot 1 = 8$$

$$4x - 12 = 3x - 5$$

$$2 \leq f(x) \leq 8 \quad J: [2; 8]$$

$$x = 7$$

3. $f(x) = \frac{2x+5}{x+1}$ funksiga $x_0 = 2$ nuqtada o'tkazilgan urinma tenglamasini yozing.

$$y = f(x_0) + f'(x_0)(x - x_0)$$

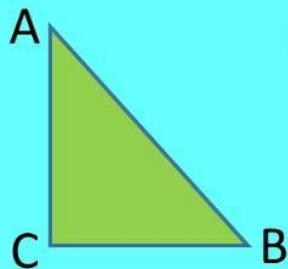
$$f(x_0) = \frac{2 \cdot 2 + 5}{2 + 1} = 3 \quad f'(x) = \frac{2(x+1) - 1(2x+5)}{(x+1)^2} = \frac{-3}{(x+1)^2}$$

$$f'(2) = \frac{-3}{(2+1)^2} = -\frac{1}{3}$$

$$y = 3 - \frac{1}{3}(x - 2) = -\frac{1}{3}x + 3\frac{2}{3}$$

$$y = -\frac{1}{3}x + 3\frac{2}{3}$$

4. To'g'ri burchakli uchburchakning gipotenuzasi 9 cm. Agar unga ichki chizilgan aylananing radiusi 5 cm bo'lsa, uchburchakning perimetrini toping.



$$AB=9 \text{ cm}, \quad r=5 \text{ cm}, \quad P=?$$

$$r = \frac{a + b - c}{2} = \frac{a + b - 9}{2} = 5$$

$$a + b - 9 = 10 \quad a + b = 19$$

$$P = a + b + c = 19 + 9 = 28 \text{ (cm)}$$

11 sinf 9 belet

9-BILET

1. Arifmetik progressiyada $S_{10} = 175$, $S_{20} = 325$ bo'lsa, S_{30} ni toping.

$$S_{10} = \frac{2a_1 + 9d}{2} \cdot 10 = 10a_1 + 45d, \quad 10a_1 + 45d = 175, \quad 2a_1 + 9d = 35$$

$$S_{20} = \frac{2a_1 + 19d}{2} \cdot 20 = 20a_1 + 190d, \quad 20a_1 + 190d = 325, \quad 4a_1 + 38d =$$

$$S_{30} = \frac{2a_1 + 29d}{2} \cdot 30 = 30a_1 + 435d,$$

$$4a_1 + 18d = 70$$

$$4a_1 + 38d = 65$$

$$2a_1 + 9 \cdot (-0,25) = 35 \quad 2a_1 = 35 + 2,25$$

$$2a_1 = 37,25 \quad a_1 = 18,625$$

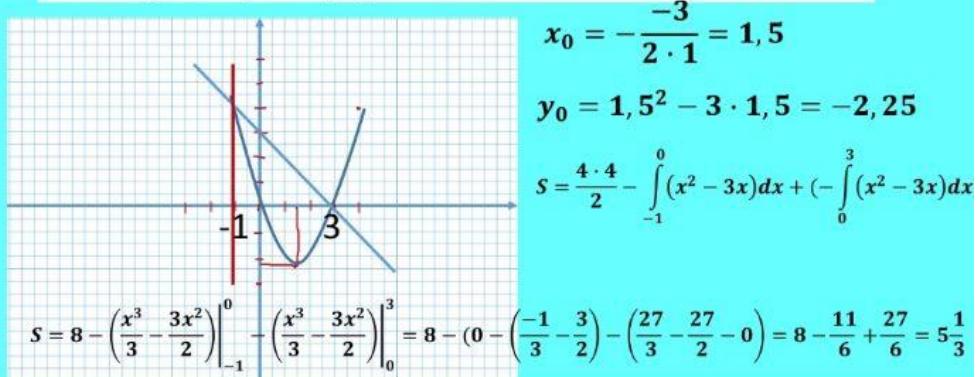
$$-20d = 5, \quad d = -0,25$$

$$S_{30} = 30 \cdot 18,625 + 435 \cdot (-0,25) = 558,75 - 108,75 = 450$$

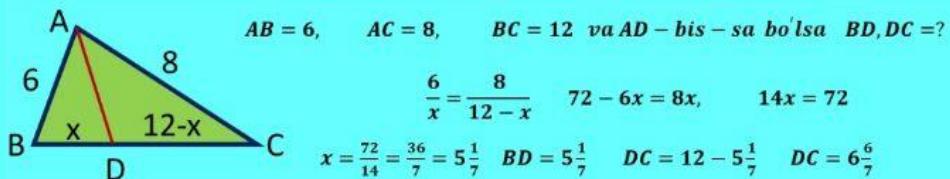
2. 30 ta o'quvchidan matematika, fizika va kimyo fan olimpiadalariga bittadan o'quvchini necha xil usulda tanlab olish mumkun?

$$\begin{array}{ccccccc} M & F & K & 1 & 2 & 3 & 1 & 1 & 3 & ? \\ \end{array} \quad 30 \cdot 29 \cdot 28 = 24360$$

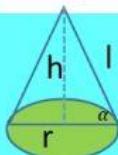
3. $f(x) = x^2 - 3x$ funksiya grafigi va $y = -x + 3$ tog'ri chiziqning kesishishidan hosil bo'lgan soha yuzini toping.



4. Tomoni 6 cm, 8 cm, 12 cm ga teng bo'lgan uchburchakning katta tomoniga tushirilgan bissektrisasi bu tomonni qanday uzunlikdagi kesmalarga ajratadi?



5. Konusning yasovchisi 25 ga, uning asos tekisligi bilan tashkil qilgan burchagini sinusi 0,6 ga teng. Konus o'q kesimining yuzini toping.



$$l = 25 \quad \sin \alpha = 0,6 \quad S_{o'q} = ?$$

$$\frac{h}{l} = \sin \alpha \quad \frac{h}{25} = 0,6 \quad h = 15, \quad r = \sqrt{25^2 - 15^2} = 20$$

$$S = \frac{1}{2} dh = \frac{1}{2} \cdot 40 \cdot 15 = 300$$